

## Speed Measures

- Time Mean Speed
- Space Mean Speed 85th Percentile Speed


## Sample Calculation of TMS and SMS



Run \#1: $\mathrm{t}_{1}=2 \mathrm{~min}, \mathrm{~d} / \mathrm{t}_{1}=60 \mathrm{miles} /$ hour
Run \#2: $\mathrm{t}_{2}=2.5 \mathrm{~min}, \mathrm{~d} / \mathrm{t}_{2}=48 \mathrm{miles} / \mathrm{hour}$
Run \#3: $\mathrm{t}_{3}=3 \mathrm{~min}, \mathrm{~d} / \mathrm{t}_{3}=40 \mathrm{miles} /$ hour
$\Sigma\left(\mathrm{d} / \mathrm{t}_{\mathrm{i}}\right)=60+48+40=148$ miles $/$ hour
TMS $=\Sigma\left(\mathrm{d} / \mathrm{t}_{\mathrm{i}}\right) / \mathrm{n}=148 / 3=49.33 \mathrm{miles} /$ hour

## Calculation of TMS and SMS

$$
\begin{aligned}
\Sigma\left(\mathrm{t}_{\mathrm{i}}\right) & =\mathrm{t}_{1}+\mathrm{t}_{2}+\mathrm{t}_{3}=2+2.5+3=7.5 \mathrm{~min} \\
\Sigma\left(\mathrm{t}_{i} / \mathrm{n}\right) & =7.5 / 3=2.5 \mathrm{~min} \\
\mathrm{SMS} & =\frac{2 \mathrm{miles} \times 60 \mathrm{~min} / \text { hour }}{2.5 \mathrm{~min}} \\
& =48 \text { miles } / \text { hour }
\end{aligned}
$$

## Spot Speed Studies در اسات النسر عة اللحظية

## > Application of Spot Speeds

1. Speed Limit Studies
2. Establishing Speed Trends
3. Specific Design Applications
4. Specific Control Applications
5. Investigation of High Accident Locations

## Spot Speed Studies در اسات السر عة اللحظية

Where to take the studies:

1. Trend locations
2. Problem locations for specific purposes
3. Representative locations for basic data surveys
4. Locations where before-and-after studies are being conducted
5. The specific location for the speed study should be selected to reduce the influence of the observer and the measuring equipment as much as possible

# Spot Speed Studies در اسات السر عة اللحظية 

## Time and duration

- The time of day for conducting a speed study depends on the purpose of the study.
- In general, when the purpose of the study is to establish posted speed limits, to observe speed trends, or to collect basic data, it is recommended that the study be conducted when traffic is freeflowing, usually during off-peak hours.
- However, when a speed study is conducted in response to citizen complaints, it is useful if the time period selected for the study reflects the nature of the complaints.


# Spot Speed Studies در اسات السر عة اللحظية 

Time and duration

- The duration of the study should be such that the minimum number of vehicle speeds required for statistical analysis is recorded.
- Typically, the duration is at least 1 hour and the sample size is at least 30 vehicles.


## Factors Affecting Spot Speeds

- Driver
- Vehicle
- Roadway
- Traffic
- Environment


## Speed Study:

## Ways to Measure Speed

Methods
Methods of Conducting Spot Speed Studies are divided into two main categories:

1. Manual
2. Automatic
$\rightarrow$ Road Detectors
$\rightarrow$ Doppler-Principle Meters
$\rightarrow$ Electronic-Principle Detectors

# Speed Study: <br> Ways to Measure Speed 

Methods (Manual)

- Spot speeds may be estimated by manually measuring the time it takes a vehicle to travel between two defined points on the roadway a known distance apart (short distance).
- Manual methods are seldom used these days.


## Speed Study: <br> Ways to Measure Speed

## Manual:

1. Using a stop watch and measuring the time it takes to travel over a specified distance
time $_{1}$
time $_{\mathbf{2}}$
Speed $=d /\left(\right.$ time $_{1}-$ time $\left._{2}\right)$

# Speed Study: <br> Ways to Measure Speed 

Methods (Automatic)

## 1. Road Detectors

$\rightarrow$ Pneumatic Road

Tubes or Induction

- An Example of a Sensor Setup of a Surface Detector Using Pneumatic Road Tubes Loops.
$\rightarrow$ Can be used to collect data on speeds at the same time as volume data are being collected.



# Speed Study: <br> <br> Ways to Measure Speed 

 <br> <br> Ways to Measure Speed}

## Methods (Automatic)

## 1. Road Detectors (contd...)

$\rightarrow$ The advantage of the detectors is that human errors are considerably reduced.
$\rightarrow$ The disadvantages are that they are expensive and may affect the driver behavior.
$\rightarrow$ Pneumatic Road Tubes are laid across the lane in which data are to be collected.

# Speed Study: <br> Ways to Measure Speed 

## Methods (Automatic)

## 1. Road Detectors (contd...)

$\rightarrow$ Tubes are usually separated by 6 ft (or could also be between 3 to 15 ft ).
$\rightarrow$ When a moving vehicle passes over the tube, an impulse is transmitted through the tube to the counter.
$\rightarrow$ The time elapsed between the two impulses and the distance between the tubes are used to compute the speed of the vehicle.

# Speed Study: <br> Ways to Measure Speed 

## Methods (Automatic)

## 1. Road Detectors (contd...)

$\rightarrow$ Induction Loops is a rectangular wire loop buried under the roadway surface.
$\rightarrow$ When a motor vehicle passes across it, an impulse is sent to the counter.

# Speed Study: Ways to Measure Speed 

## Methods (Automatic)

## 2. Doppler-Principle Meters

$\rightarrow$ Doppler meters work on the principle that when a signal is transmitted onto a moving vehicle, the change in frequency between the transmitted signal and the reflected signal is proportional to the speed of the moving vehicle.
$\rightarrow$ The difference between the frequency of the transmitted signal and that of the reflected signal is measured by the equipment, then converted to speed in mph or km/h.

## Speed Study:

## Ways to Measure Speed

## 2. Using a Radar Gun



# Speed Study: Ways to Measure Speed 

## Methods (Automatic)



Radar Gun


# Speed Study: Ways to Measure Speed 

## Methods (Automatic)

## 3. Electronic-Principle Detectors

$\rightarrow$ The presence of vehicles is detected through electronic means, and information on these vehicles is obtained, from which traffic characteristics such as speed, volume, queues, and headways are computed.
$\rightarrow$ The most promising technology using electronics is video image processing, sometimes referred to as a machine-vision system.
$\rightarrow$ One such system is the Autoscope.

## Speed Study:

## Ways to Measure Speed

Methods (Automatic)

- Real-Time Autoscope: A Fieldable Configuration



## Time Mean Speed (TMS)

Average speed of all vehicles passing a point on a highway over a specified time period

TMS $=\frac{\Sigma\left(\mathrm{d} / \mathrm{t}_{\mathrm{i}}\right)}{\mathrm{n}}(\mathrm{ft} / \mathrm{sec}$ or miles/hour)
where $\mathrm{d}=$ distance traversed (ft or mile)
$t_{i}=$ travel time of $i^{\text {th }}$ vehicle (sec or hour)
$\mathrm{n}=$ number of travel times observed

## Space Mean Speed (SMS)

## Speed corresponding to the average travel

 time over a given distance$$
\mathrm{SMS}=\frac{\mathrm{d}}{\Sigma\left(\mathrm{t}_{\mathrm{i}}\right) / \mathrm{n}}(\mathrm{ft} / \text { sec or miles/hour })
$$

where $\mathrm{d}=$ distance traversed (ft or mile)
$\mathrm{t}_{\mathrm{i}}=$ travel time of $\mathrm{ith}^{\text {th }}$ vehicle (sec or hour)
$\mathrm{n}=$ number of travel times observed

## Relationship between TMS and SMS

$$
v_{t}=v_{s}+\frac{\sigma_{s}^{2}}{v_{s}}
$$

## Data analysis

Speed Data Obtained on a Rural Highway

|  | Speed <br> $(m p h)$ | Car No. | Speed <br> $(m p h)$ | Car No. | Speed <br> $($ mph $)$ | Car No. | Speed <br> $(m p h)$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| Car No. |  |  |  |  |  |  |  |
| 1 | 35.1 | 23 | 46.1 | 45 | 47.8 | 67 | 56.0 |
| 2 | 44.0 | 24 | 54.2 | 46 | 47.1 | 68 | 49.1 |
| 3 | 45.8 | 25 | 52.3 | 47 | 34.8 | 69 | 49.2 |
| 4 | 44.3 | 26 | 57.3 | 48 | 52.4 | 70 | 56.4 |
| 5 | 36.3 | 27 | 46.8 | 49 | 49.1 | 71 | 48.5 |
| 6 | 54.0 | 28 | 57.8 | 50 | 37.1 | 72 | 45.4 |
| 7 | 42.1 | 29 | 36.8 | 51 | 65.0 | 73 | 48.6 |
| 8 | 50.1 | 30 | 55.8 | 52 | 49.5 | 74 | 52.0 |
| 9 | 51.8 | 31 | 43.3 | 53 | 52.2 | 75 | 49.8 |
| 10 | 50.8 | 32 | 55.3 | 54 | 48.4 | 76 | 63.4 |
| 11 | 38.3 | 33 | 39.0 | 55 | 42.8 | 77 | 60.1 |
| 12 | 44.6 | 34 | 53.7 | 56 | 49.5 | 78 | 48.8 |
| 13 | 45.2 | 35 | 40.8 | 57 | 48.6 | 79 | 52.1 |
| 14 | 41.1 | 36 | 54.5 | 58 | 41.2 | 80 | 48.7 |
| 15 | 55.1 | 37 | 51.6 | 59 | 48.0 | 81 | 61.8 |
| 16 | 50.2 | 38 | 51.7 | 60 | 58.0 | 82 | 56.6 |
| 17 | 54.3 | 39 | 50.3 | 61 | 49.0 | 83 | 48.2 |
| 18 | 45.4 | 40 | 59.8 | 62 | 41.8 | 84 | 62.1 |
| 19 | 55.2 | 41 | 40.3 | 63 | 48.3 | 85 | 53.3 |
| 20 | 45.7 | 42 | 55.1 | 64 | 45.9 | 86 | 53.4 |
| 21 | 54.1 | 43 | 45.0 | 65 | 44.7 |  |  |
| 22 | 54.0 | 44 | 48.3 | 66 | 49.5 |  |  |

## Data analysis

## SPEED DATA COLLECTION FORM

| SPEED GROUP (MPH) | FREQUENCY | TOTAL |
| :---: | :---: | :---: |
| 0-5 |  | 0 |
| 6-10 |  | 0 |
| 11-15 |  | 0 |
| 16-20 | N+1 | 6 |
| 21-25 | ITx 1/1 | 8 |
| 26-30 |  | 29 |
| 31-35 |  <br>  | 60 |
| 36-40 | 析 | 63 |
| 41-45 | 斯 $\operatorname{my}$ | 74 |
| 46-50 |  | 29 |
| 51-55 | ITX ITY MH III) | 19 |
| 56-60 | NVINX | 10 |
| 61-65 | // | 2 |

Weather: CLEAR On (Main Street): DIVISION
150 feet NORTH Of (Cross Street): FRANKLIN

Time (from): 3:00 (to): 3:20 PM Date: 8/15/01

## Data analysis

## Data Presentation

* The speed data can be presented by:

1. Frequency Distribution Table, and
2. Frequency and Cumulative Frequency Distribution Curves

## Data analysis

## 1. Frequency Distribution Table

- The individual speeds of vehicles collected from the field are used to prepare the frequency distribution table.
- The frequency distribution table shows the total number of vehicles observed in each speed group.
- Speed groups of more than 5 mph are not used.


## Frequency table

| speed group |  | mean group Frequency\% in(Xi) |  |  | Cumm \%fi Xi |  | $\mathrm{f}\left(\mathrm{Xi}-\mathrm{X}^{\prime}\right) \mathbf{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 15 | 13 | 0 | 0 | 0 | 0 | 0 |
| 16 | 20 | 18 | 6 | 2 | 2 | 108 | 2701 |
| 21 | 25 | 23 | 8 | 3 | 5 | 184 | 2104 |
| 26 | 30 | 28 | 29 | 10 | 15 | 812 | 3649 |
| 31 | 35 | 33 | 60 | 20 | 35 | 1980 | 2319 |
| 36 | 40 | 38 | 63 | 21 | 56 | 2394 | 93 |
| 41 | 45 | 43 | 74 | 25 | 81 | 3182 | 1059 |
| 46 | 50 | 48 | 29 | 10 | 91 | 1392 | 2237 |
| 51 | 55 | 53 | 19 | 6 | 97 | 1007 | 3610 |
| 56 | 60 | 58 | 10 | 3 | 99 | 580 | 3528 |
| 61 | 65 | 63 | 2 | 1 | 100 | 126 | 1131 |
|  |  |  | 300 | 100 |  | 11765 | 22431 |

## Statistical Calculations

## 1. Measures of Central Tendency

I. Average or Mean Speed- summation of all of the individual observations divided by the number of observations.

$$
\bar{x}=\frac{\sum n_{i} S_{i}}{N}
$$

II. Median Speed- the speed that divides the distribution into halves, i.e., there are as many drivers traveling at speeds higher than the median as are driving slower than it. On the cumulative frequency distribution curve, 50th percentile sped is the median speed.

## Statistical Calculations

## 1. Measures of Central Tendency

III.Pace- defined as the 10 mph increment in speed in which the highest percentage of drivers were observed. It is found using the frequency distribution curve.
IV. Modal Speed- the single value of speed that is most likely to occur.
$\rightarrow$ If a curve is perfectly symmetric around the mean, then the average speed, the median speed, and the modal speed are all the same.

## 85th Percentile Speed

The speed below which $85 \%$ of all traffic units travel, and above which $15 \%$ travel.

Speed limits are determined based on $85^{\text {th }}$ percentile speeds.

## Speed Statistics

| Average <br> speed | Speed data <br> Grouped <br> $\bar{u}=\frac{\sum f_{i} u_{i}}{\sum f_{i}}$ | Not grouped <br> $\bar{u}=\Sigma u_{j} / N$ |
| :--- | :--- | :--- |
| Standard <br> deviation | Speed data <br> Grouped <br> $s=\sqrt{\frac{\sum f\left(u_{i}-\bar{u}\right)^{2}}{N-1}}$ | $s=\sqrt{\frac{\sum\left(u_{j}-\bar{u}\right)^{2}}{N-1}}$ |
| Variance | $\mathrm{s}^{2}$ |  |

## Types of Speed Measurements



## Statistical Calculations

TMS $=X^{\prime}=\Sigma X i \operatorname{fi} / n=39.2 \mathrm{mph}$
Standard Deviation, $\begin{aligned} \sigma_{s}=\sqrt{\frac{\sum \mathrm{f}(\mathrm{u}-\overline{\mathrm{X}})^{2}}{\mathrm{n}-1}} & =22442 / 299 \\ & =8.66 \mathrm{mph}\end{aligned}$

Variance, $\sigma_{s}{ }^{2}=8.66^{2}=75.06 \mathrm{mph}$

## Graph Showing Percentile Speeds

2. Frequency and Cumulative Frequency Distribution Curves
$\rightarrow$ Curves are prepared from the Frequency Distribution Table.
$\rightarrow$ Once the points are plotted, they are connected by a smooth curve.
$\rightarrow$ They are usually plotted one above the other, using the same horizontal axis for speed.

## Graph Showing Percentile Speeds

$\rightarrow$ The frequency distribution curve plots points which represent the middle speed of each speed group versus the \% frequency in the speed group.
$\rightarrow$ Since the cumulative \% frequency is defined as the percentage of vehicles traveling at or below a given speed, the cumulative frequency distribution curve plots the upper limit of the speed group (NOT the middle speed).

## Graph Showing Percentile Speeds

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## Graph Showing Percentile Speeds



## Precision and confidence intervals

## Precision and Confidence Intervals

The confidence interval for the true mean is

$$
\bar{x} \pm Z E
$$

$\bar{x}=$ sample mean speed, and $\quad E=\frac{s}{\sqrt{n}}$
$s=$ sample standard deviation,$\quad n=$ sample size
$Z$ value to be calculated from Standard Normal Distributi on Table for a particular level of confidence
for $95 \%$ confidence, $\quad Z=1.96$
for $95.5 \%$ confidence, $\quad Z=2.00$
for $99.7 \%$ confidence, $\quad Z=3.00$

## Precision and confidence intervals

## Precision and Confidence Intervals

- For the example problem, standard deviation of the sample is 4.94 mph , sample size is 283 , and the sample mean speed is 48.1 mph .

$$
E=\frac{4.94}{\sqrt{283}}=0.294 \mathrm{mph}
$$

- The $95 \%$ confidence interval for the true mean speed is $48.1 \pm 1.96(0.294) \mathrm{mph}$ or from 47.52 mph to 48.68 mph.
- Therefore, we can be 95\% confident that the true mean speed would be between 47.52 mph and 48.68 mph.


## Sample size

Statistical Applications to Analyze to the Speed Distribution

Required Sample Size

$$
n=\frac{Z^{2} s^{2}}{e^{2}}
$$

$\checkmark \quad$ Where " $e$ " is the tolerance or acceptable limit of error.

## Sample size

## Required Sample Size

- Example problem: How many speeds must be measured to determine the average speed to within $\pm 1.0 \mathrm{mph}$ with $95 \%$ confidence? Assume a standard deviation of 5 mph . How many samples for a tolerance of $\pm 0.5 \mathrm{mph}$ ?
$\checkmark \quad 95 \%$ confidence, $\pm 1.0 \mathrm{mph} \rightarrow \mathrm{n}=96$ samples
$95 \%$ confidence, $\pm 0.5 \mathrm{mph} \rightarrow \mathrm{n}=384$ samples


## Before and after studies

## Before-and-After Study

* Consider the following typical situation. An accident analysis at a critical location indicates that excessive speeds are a principal causative factor in the frequent accidents. As a result, new speed limit signs are installed, and a lower limit is applied. Enforcement procedures are intensified. Six months later, speed studies at the location show some reduction in average speed.
(3) Were the new speed limit, signs, and enforcement procedures effective?


## Before and after studies

## Before-and-After Study

- To answer this question, we need to first calculate the standard deviation of the difference in means $\left(\mathrm{S}_{\mathrm{d}}\right)$ as follows

$$
S_{d}=\sqrt{\frac{s_{1}{ }^{2}}{n_{1}}+\frac{s_{2}{ }^{2}}{n_{2}}}
$$

$\rightarrow \quad$ Now if $U_{1}$ is the mean speed of the "before" study and $U_{2}$ is the mean speed of the "after" study, and if $\left|\mathrm{U}_{1}-\mathrm{U}_{2}\right|>\mathrm{ZS}_{\mathrm{d}}$, then it can be said that the mean speeds are significantly different at the confidence level corresponding to $Z$.

## Before and after studies

## Before-and-After Study

## Example

- A speed study with $n=50$ results in an average speed of 65.3 mph and a standard deviation of 5 mph . After making traffic improvements intended to reduce average speeds, a second study was made six months later. This study, with $n=60$, resulted in an average speed of 64.5 mph and a standard deviation of 6 mph . Was the observed reduction in speeds statistically significant?


## Before and after studies

## Before-and-After Study

- Standard deviation of the difference in means, $\mathrm{S}_{\mathrm{d}}$, for the given data is 1.05 mph . The " $Z$ " value for $95 \%$ confidence level is 1.96 .
- Now, $\mathrm{ZS}_{\mathrm{d}}=(1.96)(1.05)=2.058 \mathrm{mph}$
- And, $\left|U_{1}-U_{2}\right|=65.3-64.5=0.8 \mathrm{mph}$
- Since $\left|U_{1}-U_{2}\right|<Z S_{d}$, we say that at $95 \%$ confidence level, the observed reduction in average speeds is NOT statistically significant!

